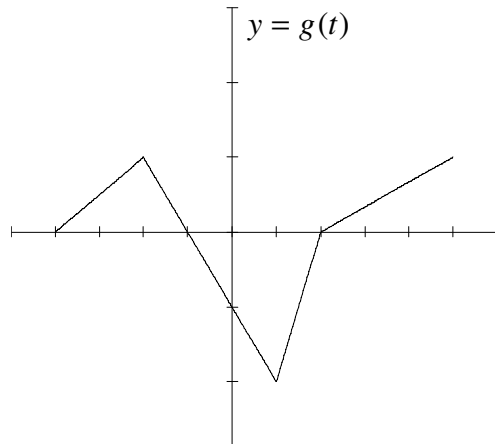


Name: _____

Investigation of the Fundamental Theorem of Calculus

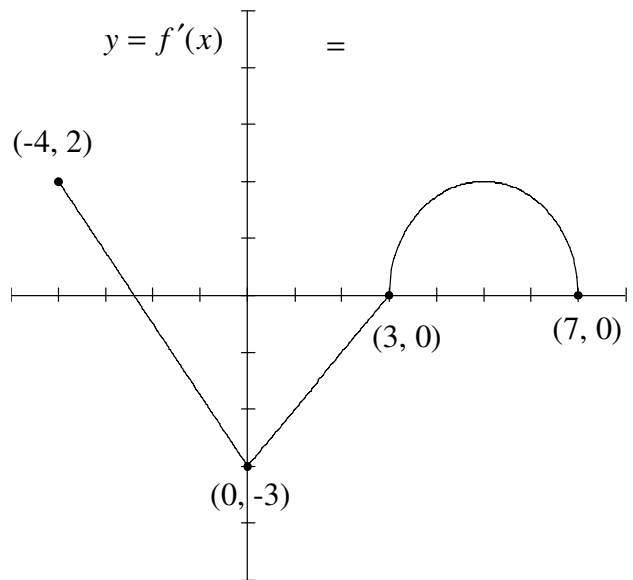
Let $f(x) = \int_0^x g(t) dt$



1. How do you evaluate the y-values for $f(x) = \int_0^x g(t) dt$

- 2. Evaluate $f(2)$. Use geometry.
- 3. Evaluate $f(-1)$. Why is your answer positive?
- 4. Find $f(5)$
- 5. Find $y = f'(x)$
- 6. What relationship do you notice between $f(x)$ and $g(t)$? Why do you think this is?
- 7. Evaluate $f''(-3)$. Show all work leading to your answer.

The graph of $y = f'(x)$ is given above consisting of two line segments and a semi-circle and $f(0) = 3$



- 8. Write an equation representing $f(x)$.
- 9. Find $f(3)$
- 10. Find $f(7)$
- 11. Find $f(-4)$
- 12. For $-4 \leq x \leq 7$, find the intervals over which $f(x)$ is increasing. Justify your answer.
- 13. For $-4 \leq x \leq 7$, find the intervals over which $f(x)$ is decreasing. Justify your answer.
- 14. Where does $f(x)$ have a relative minimum? Justify your answer.
- 15. Where is $f(x)$ concave down? Justify your answer.
- 16. What are the x -values for the points of inflection for $f(x)$? Justify your answer.